RNA Folding Algorithms with G-Quadruplexes

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Abstract. G-quadruplexes are abundant locally stable structural elements in nucleic acids. The combinatorial theory of RNA structures and the dynamic programming algorithms for RNA secondary structure prediction are extended here to incorporate G-quadruplexes using a simple but plausible energy model. With preliminary energy parameters we find that the overwhelming majority of putative quadruplex-forming sequences in the human genome are likely to fold into canonical secondary structures instead.

Key words: Dynamic programming, RNA folding, ViennaRNA Package

1 Introduction

Guanosine-rich nucleic acid sequences readily fold into four-stranded structures known as G-quadruplexes. DNA quadruplexes are, for instance, an important component of human telomeres [1], they appear to be strongly overrepresented in the promoter regions of diverse organisms, and they can associate with a variety of small molecule ligands, see [2, 3] for recent reviews. SNPs in G-quadruplexes, finally, have been implicated as a source variation of gene expression levels [4]. RNA quadruplexes have also been implicated in regulatory functions. Conserved G-quadruplex structures within the 5'-UTR of the human TRF2 mRNA [5] and eukaryotic MT3 matrix metalloproteinases, for example, repress translation [6]. Another well-studied example is the interaction of the RGG box domain fragile X mental retardation protein (FMRP) to a G-quartet-forming region in the human semaphorin 3F (S3F) mRNA [7, 8]. A recent review of G-quadruplex-based translation regulation is [9]. A functional RNA G-quadruplex in the 3' UTR was recently described as a translational repressor of the proto-oncogene PIM1 [10]. A mechanistic study of this effect, which seems to be widely used in the cell [11, 12] can be found e.g. in [13]. Most recently, G-quadruplexes were also reported in several long non-coding RNAs [14]. G-quadruplexes are potentially

Fig. 1. RNA quadruplexes form parallel arrangements with $L = 2 \dots 5$ layers. Folding energies for $L = 3$ depend mostly on the total length ℓ of the linker sequences: the data from ref. [16] fit well to an energy model of the form $\Delta G = a + b \ln \ell$ (solid line).

of functional importance in the 100 to 9000 nt G-rich telomeric repeat-containing RNAs (TERRAs) [15].

Quadruplex structures consist of stacked associations of G-quartets, i.e., planar assemblies of four Hoogsteen-bonded guanines. As in the case of base pairing, the stability of quadruplexes is derived from π -orbital interactions among stacked quartets. The centrally located cations that are coordinated by the quartets also have a major influence on the stability of quadruplex structures.

DNA quadruplexes are structurally heterogeneous: depending on the glycosidic bond angles there are 16 possible structures and further combinatorial complexity is introduced by the relative orientations of the backbone along the four edges of the stack [17]. RNA quadruplexes, in contrast, appear to be structurally monomorphic forming parallel-stranded conformations (Fig. 1, left) independently of surrounding conditions, i.e., different cations and RNA concentration [18]. Here, we restrict ourselves to the simpler case of RNA quadruplexes.

Bioinformatically, G-quadruplex structures have been investigated mostly as genomic sequence motifs. The **G4P Calculator** searches for four adjacent runs of at least three Gs. With its help a correlation of putative quadruplex forming sequences and certain functional classes of genes was detected [19]. Similarly, **quadparser** [20] recognizes the pattern (1) below. It was used e.g. in [21] to demonstrate the enrichment of quadruplexes in transcriptional regulatory regions. A substantial conservation of such sequence patterns in mammalian promoter regions is reported in [22]. The web service **QGRS Mapper** uses a similar pattern and implements a heuristic scoring system [23], see also [24] for a review. A Bayesian prediction framework based on Gaussian process regression was recently introduced to predict melting temperatures of quadruplex sequences [25].

The formation of RNA quadruplexes necessarily competes with the formation of canonical secondary structures. Hence they cannot be fully understood in isolation. In this contribution we therefore investigate how G-quadruplex structures can be incorporated into RNA secondary structure prediction algorithms.

Thermodynamic parameters for RNA quadruplexes can be derived from measurements of UV absorption as a function of temperature [26], analogous to melting curves of secondary structures. While the stability of DNA G-quadruplexes strongly depends on the arrangement of loops [27, 28] this does not appear to be the case for RNA. RNA not only forms mostly parallel-stranded stacks for G-quartets but their stability also exhibits a rather simple dependence of the loop length [16]. In further contrast to DNA [29], they appear to be less dependent on the nucleotide sequence itself.

$$G_L N_{l_1} G_L N_{l_2} G_L N_{l_3} G_L \quad (1)$$
$$E[L, \ell] = a(L - 1)g_0 + b \ln(\ell - 2) \quad (2)$$

G-quadruplex structures can be located within loops of more complex secondary structures. Fig. 2, for instance, shows the $L = 2$, $l_1 = l_2 = l_3 = 2$ quadruplex in a hairpin of the semaphorin 3F RNA [7]. It seems natural to treat G-quadruplexes inside multiloops similar to their branching helices: each

unpaired base incurs a penalty a and each G-quadruplex within a loop is associated with an additional “loop strain” b . For the interior-loop case of Fig. 2, only stabilizing mismatch contributions of the enclosing pair and a penalty for the stretches of unpaired bases are used. Sterical considerations for this case suggest that a G-quadruplex is flanked by a stretch of at least three unpaired nucleotides or has at least one unpaired nucleotide on either side.

3 Combinatorics of Structures with Quadruplexes

RNA secondary structures consist of mutually non-crossing base pairs and unpaired positions. Thus they can be represented as strings composed of matching parentheses (base pairs) and dots. This “dot-parenthesis” notation is used by the **ViennaRNA Package** [33]. G-quadruplexes constitute an extra type of structural element. The semaphorin hairpin, Fig. 2, can therefore be written as

$$\begin{aligned} &\text{GGCUGGUGAUUGGAAGGGAGGGAGGUGGCCAGCC} \\ &(((((((\dots++\dots++\dots++\dots++))))))))) \end{aligned} \quad (3)$$

using the symbol $+$ to mark the bases involved in G-quartets. This string representation uniquely identifies all G-quartets since the first run of $+$ symbols determines L for the 5'-most quadruplex, thus determining the next three G-stacks which are separated by at least one ‘.’ and must have the same length. It follows immediately that the number of secondary structures with G-quadruplexes is still smaller than 4^n , an observation that is important for the evolvability of RNAs [34]. In order to get a tighter bound on the number of structures we use here, for the sake of presentation, a simplified model in which we omit the restrictions of a minimal size of a hairpin loop and allow quadruplexes with any value of $L \geq 2$ and $l_i \geq 1$.

Let $\mathbf{g}_n$ denote the number of secondary structures with G quadruplexes on a sequence of length n . The corresponding generating function is $\mathbf{G}(x) = \sum_{n \geq 0} \mathbf{g}_n x^n$. Similarly, let $\mathbf{q}_n$ be the number of quadruplexes on length n . As derived in the supplement, its generating function is $\mathbf{Q}(x) = \sum_{n \geq 0} \mathbf{q}_n x^n = x^{11}(1-x)^{-3}(1-x^4)^{-1}$. The basic idea is now to consider a structure consisting of b base pairs, u unpaired bases and k quadruplexes. Then there are $\binom{2b+k}{k}$ ways to insert k quadruplexes into each of the $C_b = \frac{1}{b+1} \binom{2b}{b}$ possible arrangements of b matching pairs of parentheses. Into each of these arrangements we can insert u unpaired bases in $\binom{2b+k+u}{u}$ different ways. Thus we have

$$\begin{aligned} \mathbf{G}(x) &= \sum_k \sum_b \sum_u \frac{1}{b+1} \binom{2b}{b} \binom{2b+k}{k} \binom{2b+k+u}{u} x^{2b+u} \mathbf{Q}(x)^k \\ &= \frac{2}{1-x-\mathbf{Q}(x) + \sqrt{(1-3x-\mathbf{Q}(x))(1+x-\mathbf{Q}(x))}} \end{aligned} \quad (4)$$

Following [35] we find that the coefficients of $\mathbf{G}(x)$ are asymptotically given by $\mathbf{g}_n \sim k_0 n^{-3/2} \gamma^n$, where k_0 is a positive constant and $\gamma \approx 3.00005$. A more detailed model accounting for minimal stack and loop lengths is analyzed in the

Fig. 3. Extension of recursions of the **ViennaRNA Package** to accomodate G-quadruplexes. This grammar treats G-quadruplexes with multi-loop like energies also in an interior-loop-like context.

Supplemental Material. It yields $\gamma \approx 2.2903$ if isolated base pairs are allowed, and $\gamma \approx 1.8643$ for canonical secondary structures.

4 RNA Folding Algorithms

Energy Minimization. Dynamic programming algorithms for secondary structure prediction are based on a simple recursive decomposition: any feasible structure on the interval $[i, j]$ has the first base either unpaired or paired with a position k satisfying $i < k \leq j$. The condition that base pairs do not cross implies that the intervals $[i + 1, k - 1]$ and $[k + 1, j]$ form self-contained structures whose energies can be evaluated independent of each other. In conjunction with the standard energy model [36], which distinguishes hairpin loops, interior loops (including stacked base pairs), and multi-loops, this leads to the recursions diagrammatically represented in Fig. 3 (ignoring the cases involving black blocks). This algorithmic approach was pioneered e.g. in [37, 38] and is also used in the **ViennaRNA Package** [33].

G-quadruplexes form closed structural elements on well-defined sequence intervals. Thus they can be treated just like substructures enclosed by a base pair, so that the additional ingredients in the folding algorithms are the energies G_{ij} (free energy of the most stable quadruplex so that the pattern (1) matches exactly the interval $[i, j]$) and the partition functions Z_{ij}^G (defined as the sum of the Boltzmann factors of all distinct quadruplexes on the interval $[i, j]$). As a consequence of (1) we have $G_{ij} < \infty$ and $Z_{ij}^G > 0$ only if $|j - i| < 4L_{\max} + \ell_{\max}$. All possible quadruplexes on the interval $[i, j]$ can be determined and evaluated in $\mathcal{O}(L_{\max}^2 \ell_{\max}^2)$ time so that these arrays can be pre-computed in $\mathcal{O}(n(L_{\max} + \ell_{\max})L_{\max}^2 \ell_{\max}^2)$, i.e., in linear time.

The standard recursions for RNA secondary structure prediction can now be extended by extra terms for quadruplexes, see Fig. 3. The simplest strategy

would be to add G-quadruplexes as an additional type of base-pair enclosed structures. This would amount to using standard interior loop parameters also for cases such as Fig. 2. Hence we use the somewhat more elaborate grammar of Fig. 3, which introduces the quadruplexes in the form of additional cases into the multi-loop decomposition. An advantage of this method is that one can use different parameter values to penalize the inclusion of quadruplexes and helical components into a multiloop. Clearly the grammar is still unambiguous, i.e., every structure has an unique parse. Thus it can be used directly to compute partition functions.

Base Pairing Probabilities. A straightforward generalization of McCaskill’s algorithm can be used to compute the probabilities P_{ij} of all possible base pairs (i, j) . The probability P_{ij}^G of finding a G-quadruplex delimited by positions i and j then can be written as

$$P_{ij}^G = \frac{Z_{1,i-1} Z_{ij}^G Z_{j+1,n}}{Z} + \sum_{\substack{k < i-1 \\ l > j+1}} P_{kl} \mathbb{P} \{ \text{quadruplex}[i, j] | (k, l) \} \quad (5)$$

The conditional probabilities $\mathbb{P}\{\dots\}$ in turn are composed of the four individual cases depending on the placement of the components of the generalized multiloop enclosed by (k, l) relative to the interval $[i, j]$:

This decomposition translates to the recursion $\mathbb{P} \{ \text{quadruplex}[i, j] | (k, l) \} =$

$$\frac{Z_{k+1,i-1}^M Z_{ij}^G Z_{j+1,l-1}^M}{Z_{kl}^B} + \frac{Z_{k+1,i-1}^M Z_{ij}^G \hat{b}^{l-j-1}}{Z_{kl}^B} + \frac{\hat{b}^{i-k-1} Z_{ij}^G Z_{j+1,l-1}^M}{Z_{kl}^B} + \frac{\hat{b}^{i-k-1} Z_{ij}^G \hat{b}^{l-j-1}}{Z_{kl}^B}$$

where $\hat{b} = \exp(-b/RT)$. From the P_{ij}^G it is straightforward to compute the probability of a particular quadruplex as

$$p([i, L, l_1, l_2, j]) = \frac{\exp(-E[L, \ell])}{Z_{ij}^G} P_{ij}^G \quad (7)$$

where $l_3 = j - i + 1 - 4L - l_1 - l_2$. Summing up the probabilities of all quadruplexes that contain a particular contact $i' : j'$ of two guanosines in a layer finally yield the probability of the G:G contact $i' : j'$.

Fig. 4 shows an example of the graphical output of `RNAfold`. In the minimum energy case we use a very simple modification of the standard layout [39] treating each quadruplex like a local hairpin structure, explicitly indicating the G-G pairs. Quadruplexes are shown in addition to the individual G-G pairs as shaded triangles in the base pair probability dot plots. From the base pairing probabilities we also compute MEA [40] and centroid structures.

Fig. 4. Representation of minimum free energy structure (l.h.s.) and base pairing probability matrix (r.h.s.) of the semaphorin hairpin (see Fig. 2) respectively.

By definition the centroid structure X minimizes the expected base pair distance to the other structures within the Boltzmann-weighted ensemble. In the absence of G-quadruplexes X consists of all base pairs (i, j) with $p_{ij} > 1/2$. A certain ambiguity arises depending on whether X is interpreted as a list of base pairs that may contain incomplete quadruplexes, or whether quadruplexes are treated as units. Here, we insert a quadruplex if $P_{ij}^G > 0.5$, and represent it by the most stable quadruplex with endpoints i and j . The same representation is used for MEA structures where we extend the maximized expected accuracy to $EA = \sum_{(i,j) \in S} 2\gamma(P_{i,j} + P_{ij}^G) + \sum_i P_i^u$ with $P_i^u = 1 - \sum_j P_{ij} - \sum_{k \leq i \leq l} P_{kl}^G$, accordingly.

Consensus Structures can be readily obtained for a given multiple sequence alignment. The idea is to apply the dynamic programming recursions to alignment columns. The energy contributions are determined as the average of the corresponding contributions to the individual sequences [42]. In addition small contributions are added to favor pairs of columns with consistent (e.g. GC→GU) and compensatory mutations (AU→GC) since these provide direct evidence for selection acting to preserve base pairing. Similarly, penalties are added if one or a few sequences cannot form a base pair. We refer to [43] for details of the scoring model implemented in *RNAalifold*. Here, we extend it by a simple system of penalties for mutations that disrupt quadruplexes. Non-G nucleotides incur an energy E' in the outer layers of the quadruplex and $2E'$ in the inner layers as they affect one or two stacking interactions, respectively. An example of a consensus structure prediction is shown in Fig. 5.

Implementation Details. The implementation of G-quadruplex folding in *RNAfold* and *RNAalifold* essentially follows the extended grammar shown in Fig. 3, distinguishing the energy contribution of unpaired bases in the external loop from those enclosed by base pairs. The energies of all possible G-quadruplexes are pre-computed, storing the energy of the most stable quadruplex

Fig. 5. Consensus structure of the 5'-most part of the 5'UTR of the NRAS mRNA, exhibiting a conserved G-quadruplex with $L = 3$ that modulates translation of the NRAS proto-oncogene [41]. Colors indicate the number (red 1, ochre 2, green 3) of different types of basepairs in a pair of alignment columns, unsaturated colors indicate basepairs that cannot be formed by 1 or 2 sequences. Substitutions in stem regions are indicated by circles in the secondary structure drawing.

for each pair of endpoints in the triangular matrix G . As this matrix will be very sparse for most inputs, a sparse matrix optimization is possible, but not yet implemented. In the backtracing part we re-enumerate quadruplexes with given endpoints whenever necessary. Base pairing probabilities are computed as outlined above. Since there cannot be a conflict with canonical base pairs, we store P_{ij}^G as part of the base pairing probability matrix. The probabilities of individual G-G contacts are computed by enumeration as a post-processing step. We also adapted the RNAeval and RNApilot programs so that sequence/structure pairs can be parsed and re-evaluated according to the extended grammar.

5 Evaluation

Runtime Performance. The runtime of RNAfold with the extended grammar of Fig. 3 was compared to the implementation of the standard model. For both, energy minimization and partition function, virtually no difference was observed. For short sequences of about 200 nt the additional pre-processing steps incur a minor but negligible runtime overhead.

Occurrence and stability of G-quadruplexes in genomes. Sequence motifs of the form (1) that can in principle form quadruplex structures are very abundant in most genomes, see e.g. [19–21]. The number of putative quadruplex-forming sequences is even slightly larger than expected from random sequences with the same mono- or dinucleotide distributions, Fig. 6. The overwhelming majority of these quadruplex candidates, however, is unstable compared to canonical secondary structures that use some or all of Gs in canonical base pairs. We observe that less than 2% of the putative quadruplexes are thermodynamically stable. Interestingly, this effect is nearly independent of the number of layers (L). This data is preliminary, since it is based on energy parameters that have

Fig. 6. Abundance and stability of putative G-quadruplexes. L.h.s.: Box plot showing the number of potential G-quadruplexes in human chromosome 2 within sliding windows of 500 000 nucleotides. For comparison, the same information for a random sequence with the same mono- or di-nucleotide composition than chr. 2 is presented as well. Both, the mono- and di-nucleotide distribution have been generated from chromosome 2. **RNAfold** denotes the number of putative G-quadruplexes stable enough to occur in a predicted structure of 100 nucleotides up- and downstream of the putative G-quadruplex (with median=1, interquartile range=0–2). R.h.s.: fraction of stable quadruplexes as function of L for human chromosome 2.

been fitted on a rather limited amount of empirical evidence and do not include the important issues arising from the strong dependence of quadruplex stability of cation concentrations. Furthermore, it reflects the occurrence of putative G-quadruplexes on the human chromosome 2 only. More comprehensive and accurate parameters as well as a local folding algorithm that extends **RNAfold** [44] will be subject of a forthcoming study. Several experimentally known RNA quadruplexes are predicted by the current version, including the semaphorin hairpin of Fig. 4 and the quadruplex in human telomerase RNA [45] discussed in the Supplemental Material.

6 Discussion

We have shown in this contribution that structural elements such as G-quadruplexes that correspond to uninterrupted sequence intervals can be included in a rather straightforward way into the standard dynamic programming recursions – provided a corresponding extension of the energy model can be devised. The G-quadruplex-aware programs are currently available as a separate branch (version number with the suffix "g") of the **ViennaRNA Package** using a very simple energy function for the quadruplexes that reproduces the few available experimental data at least semi-quantitatively. Following further optimization of the code the algorithmic extensions will be integrated in the main version of the package in the near future. The extensions in Fig. 3 can also be applied to local folding algorithms such as **RNAfold** and **RNAplfold** or the exhaustive

enumeration of suboptimal structures in `RNAsubopt`. This is ongoing work, as is a comprehensive set of tools for genome-wide scans for putative G-quadruplexes.

It is less obvious how to handle quadruplexes in RNA-RNA interactions since our recursions consider local G-quadruplexes only. At least it is clear that they can be included in all those parts of the structure that are not involved in intermolecular contacts. Some quadruplex structures, however, are formed *in trans*. The binding of G-rich small RNAs to G-rich regions in reporter mRNAs leads to the formation of an intermolecular RNA G-quadruplex that in turn can inhibit translation in living cells [46]. One can use `RNAup` [47] to compute the probabilities $p^{(1)}$ and $p^{(2)}$ that the G-rich regions are unpaired. From these, we obtain the free energies $G^{(i)} = -RT \ln p^{(i)}$ to make the binding site accessible. It remains to compute the interaction energy itself.

The main problem for practical applications of quadruplex-aware RNA folding tools is our limited knowledge of the energy function in particular for $L \neq 3$ and for asymmetric linkers. Even with the crude energy function employed here it becomes clear that the overwhelming majority of putative genomic quadruplex sequences will fold into a canonical secondary structure rather than G-quadruplex structures.

Supplemental Material and Source Code are available from <http://www.bioinf.uni-leipzig.de/publications/supplements/12-006> and www.tbi.univie.ac.at/~ronny/programs/.

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